Oscillator

- Introduction of Oscillator
- Linear Oscillator
 - Wien Bridge Oscillator
 - RC Phase-Shift Oscillator
 - LC Oscillator
- Stability

Oscillators

Oscillation: an effect that repeatedly and regularly fluctuates about the mean value

Oscillator: circuit that produces oscillation

Characteristics: wave-shape, frequency, amplitude, distortion, stability

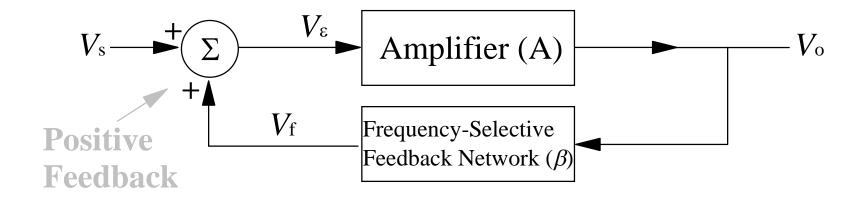
Application of Oscillators

- Oscillators are used to generate signals, e.g.
 - Used as a local oscillator to transform the RF signals to IF signals in a receiver;
 - Used to generate RF carrier in a transmitter
 - Used to generate clocks in digital systems;
 - Used as sweep circuits in TV sets and CRO.

Linear Oscillators

- 1. Wien Bridge Oscillators
- 2. RC Phase-Shift Oscillators
- 3. LC Oscillators
- 4. Stability

Integrant of Linear Oscillators



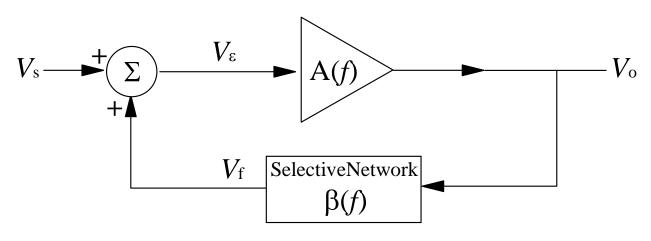
For sinusoidal input is connected

"Linear" because the output is approximately sinusoidal

A linear oscillator contains:

- a frequency selection feedback network
- an amplifier to maintain the loop gain at unity

Basic Linear Oscillator



$$V_o = AV_\varepsilon = A(V_s + V_f)$$
 and $V_f = \beta V_o$

$$\Rightarrow \frac{V_o}{V_s} = \frac{A}{1 - A\beta}$$

If $V_s = 0$, the only way that V_o can be nonzero is that loop gain $A\beta=1$ which implies that

$$|A\beta|=1$$
 (Barkhausen Criterion)
 $\angle A\beta=0$

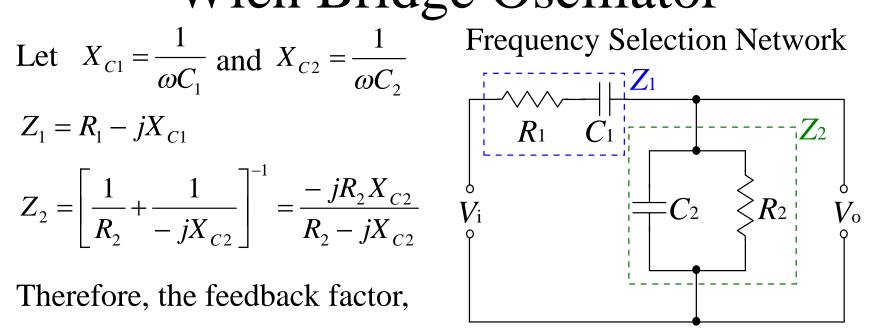
Wien Bridge Oscillator

Let
$$X_{C1} = \frac{1}{\omega C_1}$$
 and $X_{C2} = \frac{1}{\omega C_2}$

$$Z_1 = R_1 - jX_{C1}$$

$$Z_{2} = \left[\frac{1}{R_{2}} + \frac{1}{-jX_{C2}}\right]^{-1} = \frac{-jR_{2}X_{C2}}{R_{2} - jX_{C2}}$$

Therefore, the feedback factor,



$$\beta = \frac{V_o}{V_i} = \frac{Z_2}{Z_1 + Z_2} = \frac{(-jR_2X_{C2}/R_2 - jX_{C2})}{(R_1 - jX_{C1}) + (-jR_2X_{C2}/R_2 - jX_{C2})}$$

$$\beta = \frac{-jR_2X_{C2}}{(R_1 - jX_{C1})(R_2 - jX_{C2}) - jR_2X_{C2}}$$

 β can be rewritten as:

$$\beta = \frac{R_2 X_{C2}}{R_1 X_{C2} + R_2 X_{C1} + R_2 X_{C2} + j(R_1 R_2 - X_{C1} X_{C2})}$$

For *Barkhausen Criterion*, imaginary part = 0, i.e.,

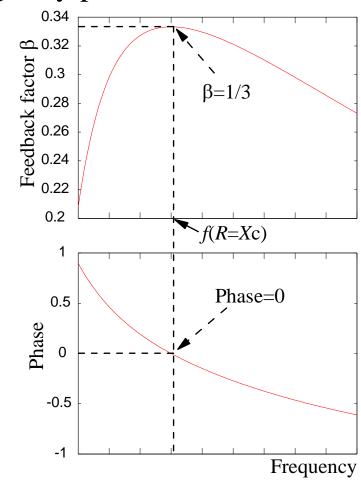
$$R_1 R_2 - X_{C1} X_{C2} = 0$$
or
$$R_1 R_2 = \frac{1}{\omega C_1} \frac{1}{\omega C_2}$$

$$\Rightarrow \omega = 1/\sqrt{R_1 R_2 C_1 C_2}$$

Supposing,

$$R_1 = R_2 = R$$
 and $X_{C1} = X_{C2} = X_C$,

$$\beta = \frac{RX_C}{3RX_C + j(R^2 - X_C^2)}$$



By setting $\omega = \frac{1}{RC}$ Example, we get

Imaginary part = 0 and $\beta = \frac{1}{3}$

Due to Barkhausen Criterion,

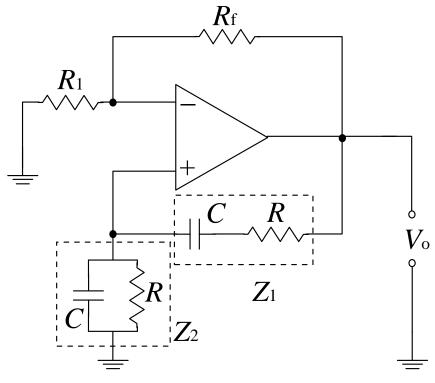
Loop gain $A_{\nu}\beta=1$

where

 $A_{\rm v}$: Gain of the amplifier

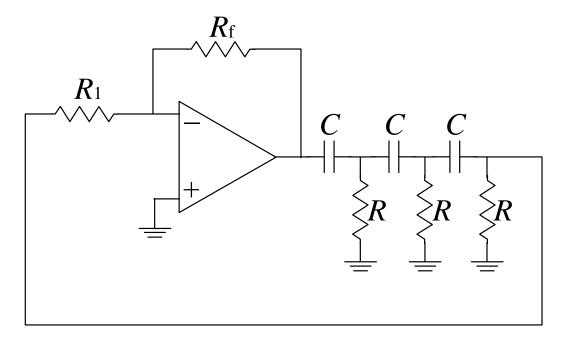
$$A_{\nu}\beta = 1 \Rightarrow A_{\nu} = 3 = 1 + \frac{R_f}{R_1}$$

Therefore, $\frac{R_f}{R_1} = 2$



Wien Bridge Oscillator

RC Phase-Shift Oscillator



- Using an inverting amplifier
- The additional 180° phase shift is provided by an RC phase-shift network

Applying KVL to the phase-shift network, we have

$$V_1 = I_1(R - jX_C) - I_2R$$

 $0 = -I_1R$ $+I_2(2R - jX_C) - I_3R$
 $0 = -I_2R$ $+I_3(2R - jX_C)$
Solve for I_3 , we get

$$I_{3} = \begin{vmatrix} R - jX_{C} & -R & V_{1} \\ -R & 2R - jX_{C} & 0 \\ 0 & -R & 0 \end{vmatrix}$$

$$R - jX_{C} & -R & 0 \\ -R & 2R - jX_{C} & -R \\ 0 & -R & 2R - jX_{C} \end{vmatrix}$$

Or
$$I_3 = \frac{V_1 R^2}{(R - jX_C)[(2R - jX_C)^2 - R^2] - R^2(2R - jX_C)}$$

The output voltage,

$$V_o = I_3 R = \frac{V_1 R^3}{(R - jX_C)[(2R - jX_C)^2 - R^2] - R^2(2R - jX_C)}$$

Hence the transfer function of the phase-shift network is given by,

$$\beta = \frac{V_o}{V_1} = \frac{R^3}{(R^3 - 5RX_C^2) + j(X_C^3 - 6R^2X_C)}$$

For 180° phase shift, the imaginary part = 0, i.e.,

$$X_C^3 - 6R^2 X_C = 0$$
 or $X_C = 0$ (Rejected)

$$\Rightarrow X_C^2 = 6R^2$$

$$\omega = \frac{1}{\sqrt{6}RC}$$

and,

$$\beta = -\frac{1}{29}$$

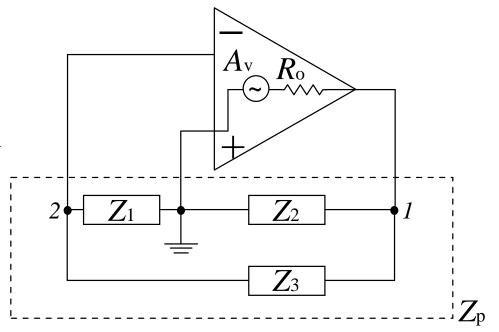
Note: The –ve sign mean the phase inversion from the voltage

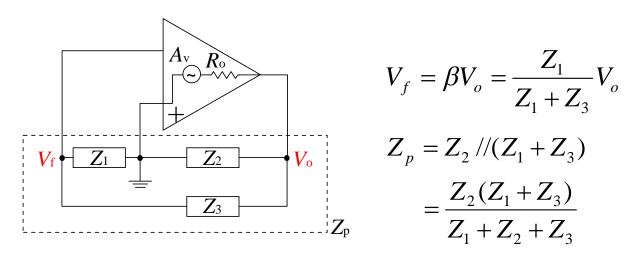
LC Oscillators

- The frequency selection network $(Z_1, Z_2 \text{ and } Z_3)$ provides a phase shift of 180°
- The amplifier provides an addition shift of 180°

Two well-known Oscillators:

- Colpitts Oscillator
- Harley Oscillator





For the equivalent circuit from the output

Therefore, the amplifier gain is obtained,

$$A = \frac{V_o}{V_i} = \frac{-A_v Z_2 (Z_1 + Z_3)}{R_o (Z_1 + Z_2 + Z_3) + Z_2 (Z_1 + Z_3)}$$

The loop gain,

$$A\beta = \frac{-A_{v}Z_{1}Z_{2}}{R_{o}(Z_{1} + Z_{2} + Z_{3}) + Z_{2}(Z_{1} + Z_{3})}$$

If the impedance are all pure reactances, i.e.,

$$Z_1 = jX_1$$
, $Z_2 = jX_2$ and $Z_3 = jX_3$

The loop gain becomes,
$$A\beta = \frac{A_{v}X_{1}X_{2}}{jR_{o}(X_{1} + X_{2} + X_{3}) - X_{2}(X_{1} + X_{3})}$$

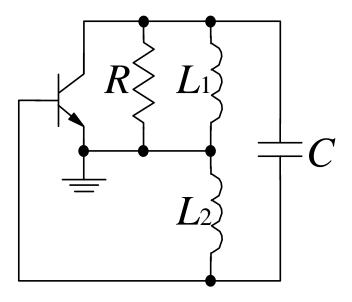
The imaginary part = 0 only when $X_1 + X_2 + X_3 = 0$

- It indicates that at least one reactance must be –ve (capacitor)
- X_1 and X_2 must be of same type and X_3 must be of opposite type

With imaginary part = 0,
$$A\beta = \frac{-A_v X_1}{X_1 + X_3} = \frac{A_v X_1}{X_2}$$

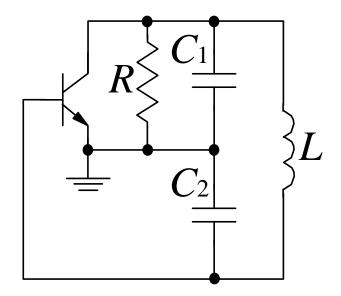
For Unit Gain & 180° Phase-shift,
$$A\beta = 1 \implies A_{\nu} = \frac{X_2}{X_1}$$

Hartley Oscillator



$$\omega_o = \frac{1}{\sqrt{(L_1 + L_2)C}}$$
$$g_m = \frac{L_1}{RL_2}$$

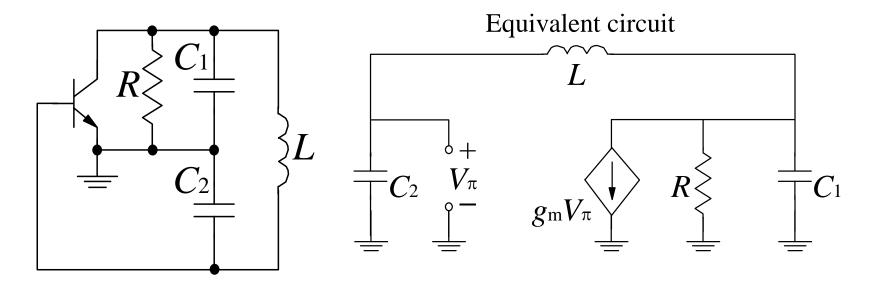
Colpitts Oscillator



$$\omega_o = \frac{1}{\sqrt{LC_T}} \qquad C_T = \frac{C_1 C_2}{C_1 + C_2}$$

$$g_m = \frac{C_2}{RC_1}$$

Colpitts Oscillator



In the equivalent circuit, it is assumed that:

- Linear small signal model of transistor is used
- The transistor capacitances are neglected
- Input resistance of the transistor is large enough

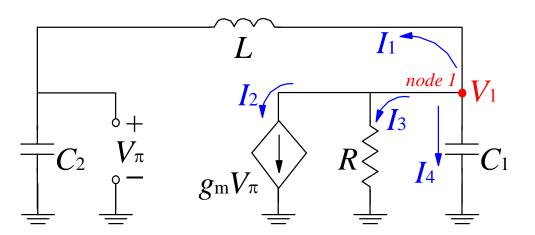
At node 1,

$$V_1 = V_{\pi} + i_1(j\omega L)$$

where,

$$i_1 = j\omega C_2 V_{\pi}$$

$$\Rightarrow V_1 = V_{\pi} (1 - \omega^2 L C_2)$$



Apply KCL at node 1, we have

$$j\omega C_{2}V_{\pi} + g_{m}V_{\pi} + \frac{V_{1}}{R} + j\omega C_{1}V_{1} = 0$$

$$j\omega C_{2}V_{\pi} + g_{m}V_{\pi} + V_{\pi}(1 - \omega^{2}LC_{2})\left(\frac{1}{R} + j\omega C_{1}\right) = 0$$

For Oscillator V_{π} must not be zero, therefore it enforces,

$$\left(g_{m} + \frac{1}{R} - \frac{\omega^{2}LC_{2}}{R}\right) + j\left[\omega(C_{1} + C_{2}) - \omega^{3}LC_{1}C_{2}\right] = 0$$

$$\left(g_{m} + \frac{1}{R} - \frac{\omega^{2}LC_{2}}{R}\right) + j\left[\omega(C_{1} + C_{2}) - \omega^{3}LC_{1}C_{2}\right] = 0$$

Imaginary part = 0, we have

$$\omega_o = \frac{1}{\sqrt{LC_T}} \qquad C_T = \frac{C_1 C_2}{C_1 + C_2}$$

Real part = 0, yields

$$g_m = \frac{C_2}{RC_1}$$

Frequency Stability

• The frequency stability of an oscillator is defined as

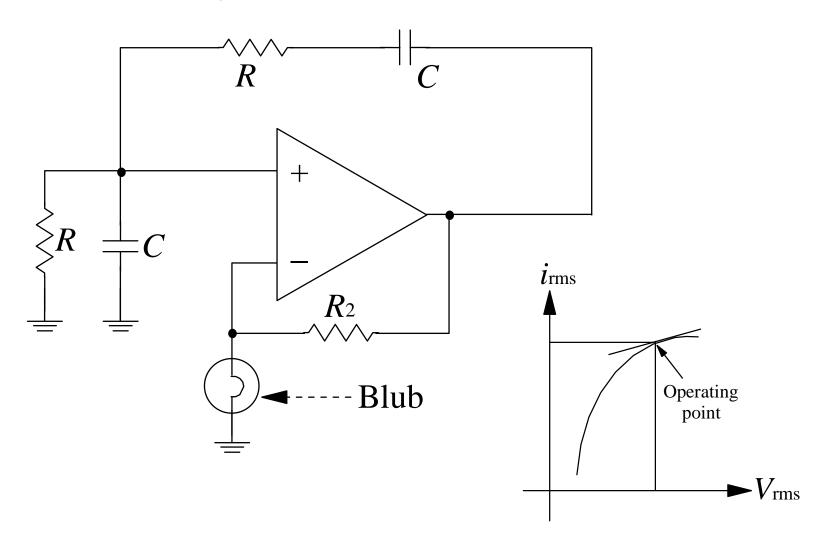
$$\frac{1}{\omega_o} \cdot \left(\frac{d\omega}{d\mathbf{T}}\right) \omega = \omega_o \qquad \mathbf{ppm}/^{\mathbf{o}}\mathbf{C}$$

• Use high stability capacitors, e.g. silver mica, polystyrene, or teflon capacitors and low temperature coefficient inductors for high stable oscillators.

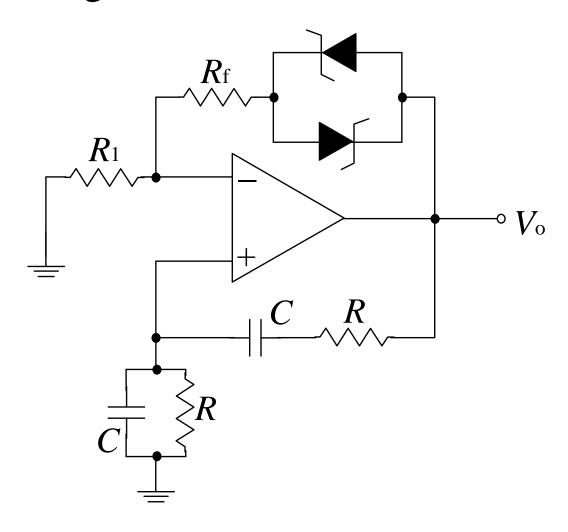
Amplitude Stability

- In order to start the oscillation, the loop gain is usually slightly greater than unity.
- LC oscillators in general do not require amplitude stabilization circuits because of the selectivity of the LC circuits.
- In RC oscillators, some non-linear devices, e.g. NTC/PTC resistors, FET or zener diodes can be used to stabilized the amplitude

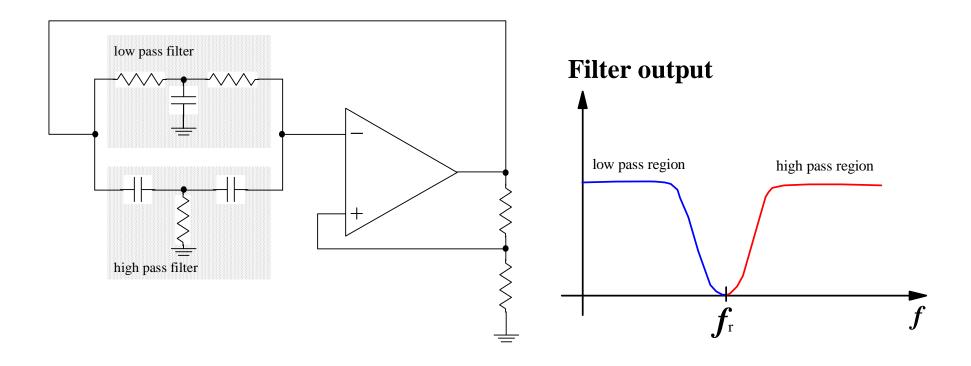
Wien-bridge oscillator with bulb stabilization



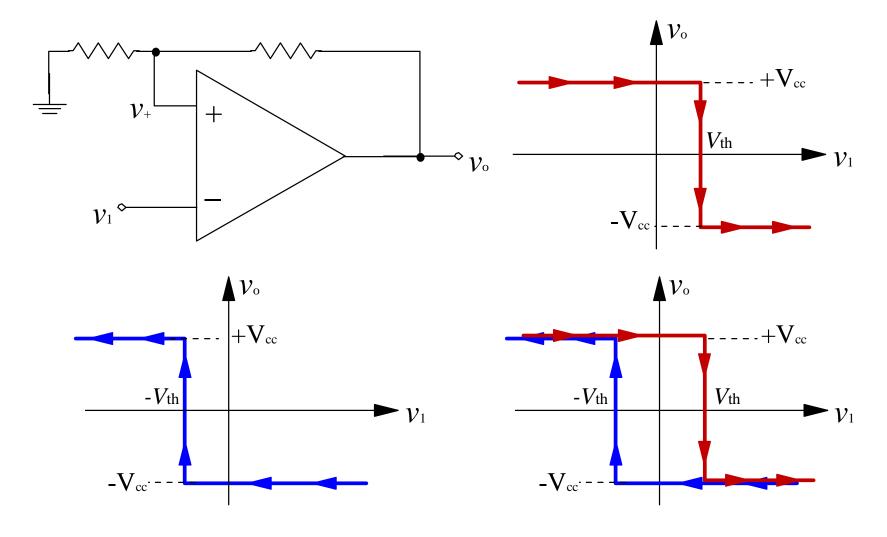
Wien-bridge oscillator with diode stabilization



Twin-T Oscillator



Bistable Circuit



A Square-wave Oscillator

